

# Line shape models in magnetic fusion research and astrophysics

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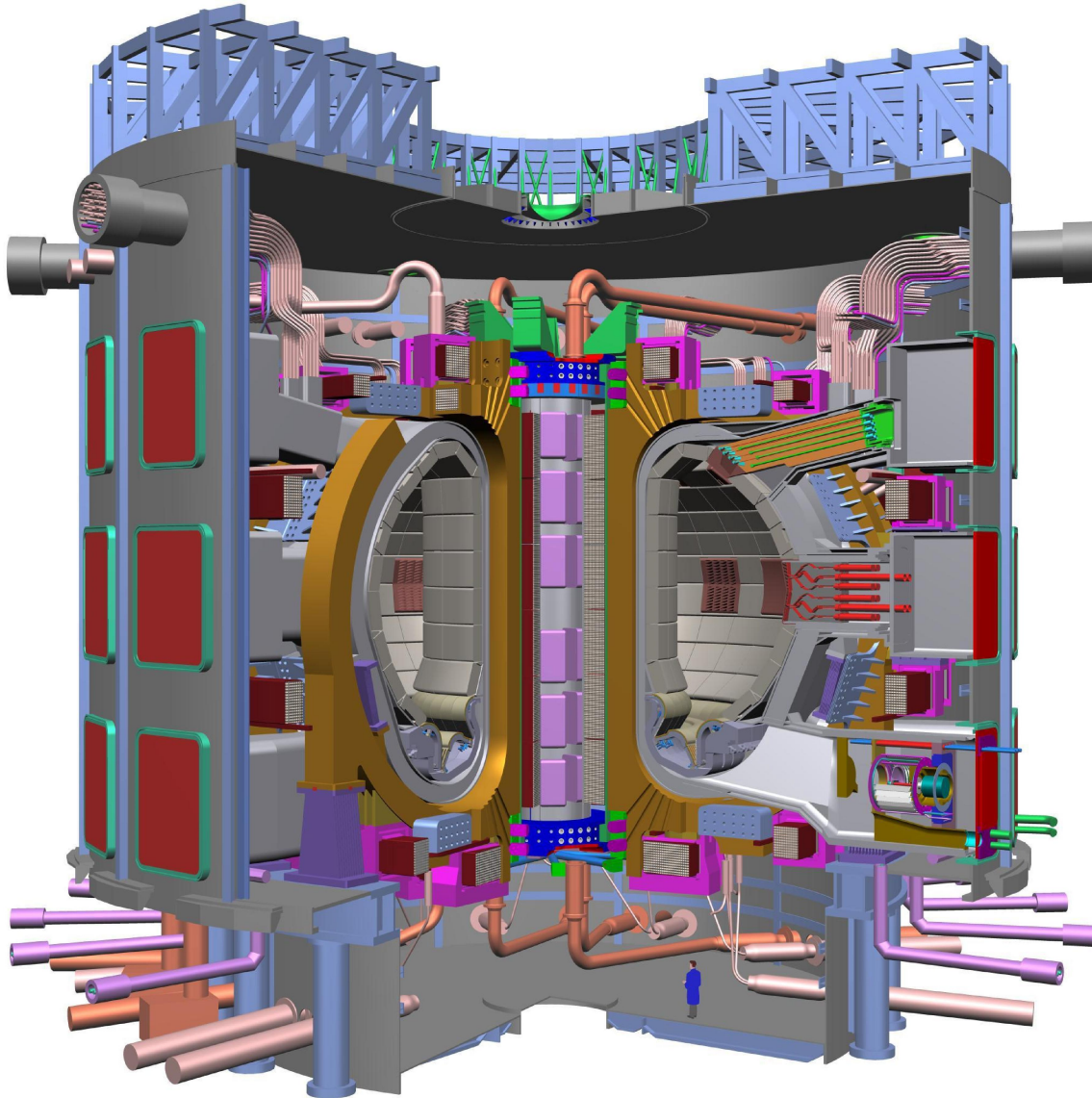
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# Outline

- 1) The ITER project: an overview
- 2) Passive spectroscopy of current tokamak plasmas: line shapes, Stark broadening and Zeeman effect
- 3) Applying line shape models to stellar atmosphere spectra analysis

# The ITER project ([www.iter.org](http://www.iter.org))



Aim: demonstrate the feasibility of the fusion power

An international collaboration

- 1<sup>st</sup> controlled fusion burning plasma
- Presently under construction (France)
- First plasma in 2025

# The ITER project ([www.iter.org](http://www.iter.org))



# Research activities in France and in Europe

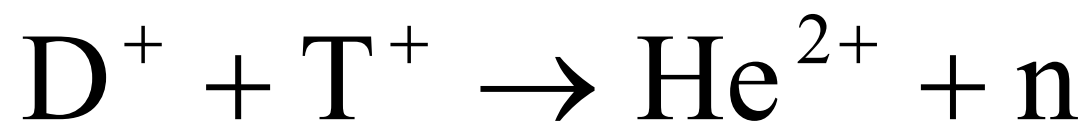
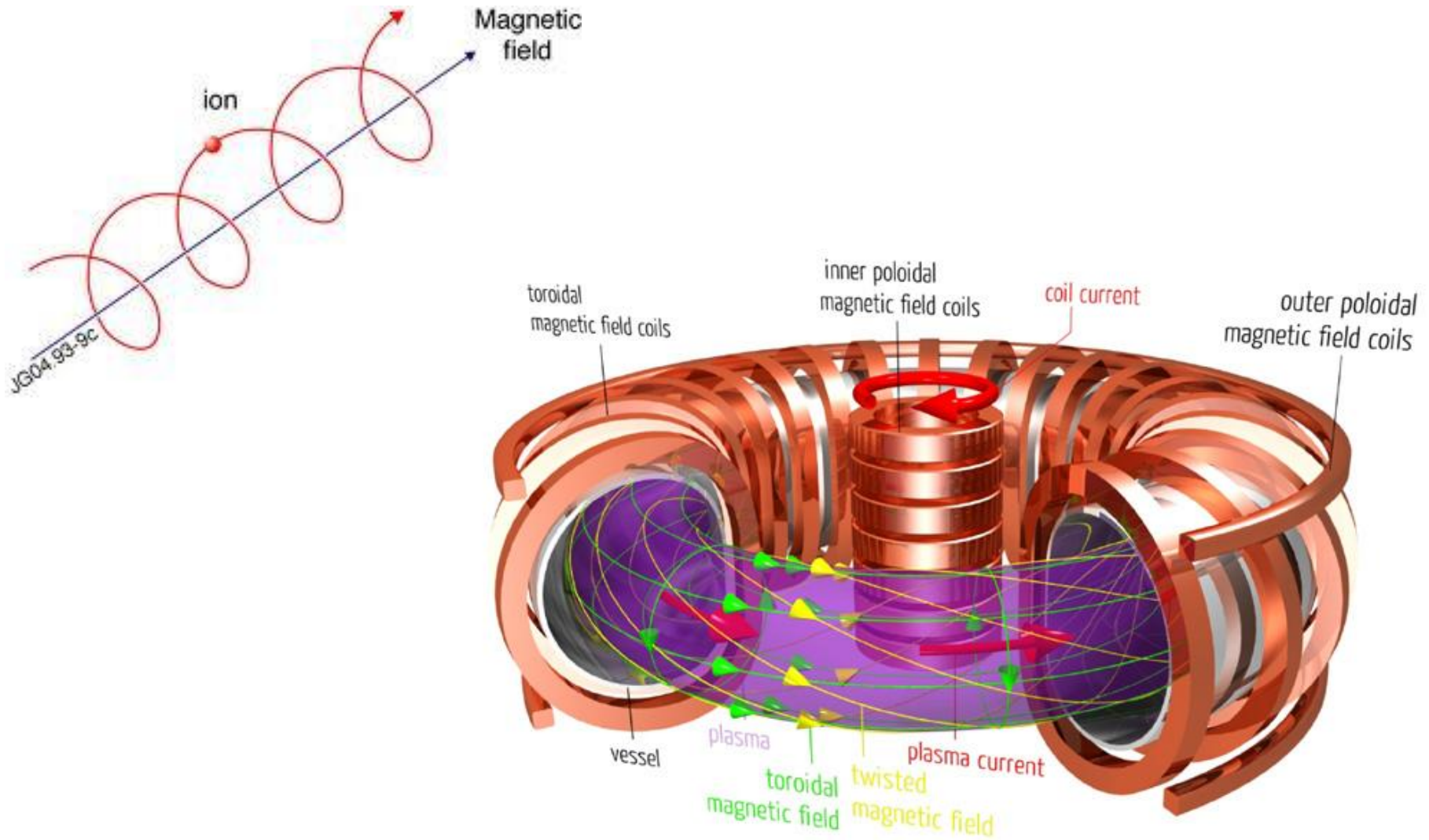


From [www.euro-fusion.org](http://www.euro-fusion.org):

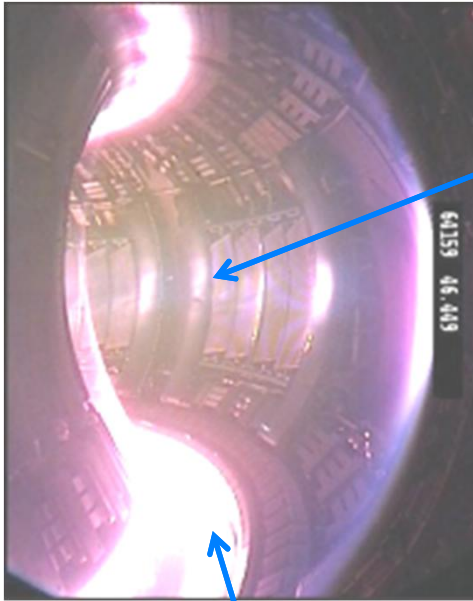
“EUROfusion funds fusion research activities in accordance with the *Roadmap to the realisation of fusion energy*. The Roadmap outlines the most efficient way to realise fusion electricity by 2050.”



# ITER is a tokamak



# Presentation of tokamak plasmas



Center:

- $T_e, T_i$  up to 10 keV
- fully ionized H plasma
- presence of multicharged impurity ions

Electron densities range in  $\sim 10^{12} - 10^{15} \text{ cm}^{-3}$

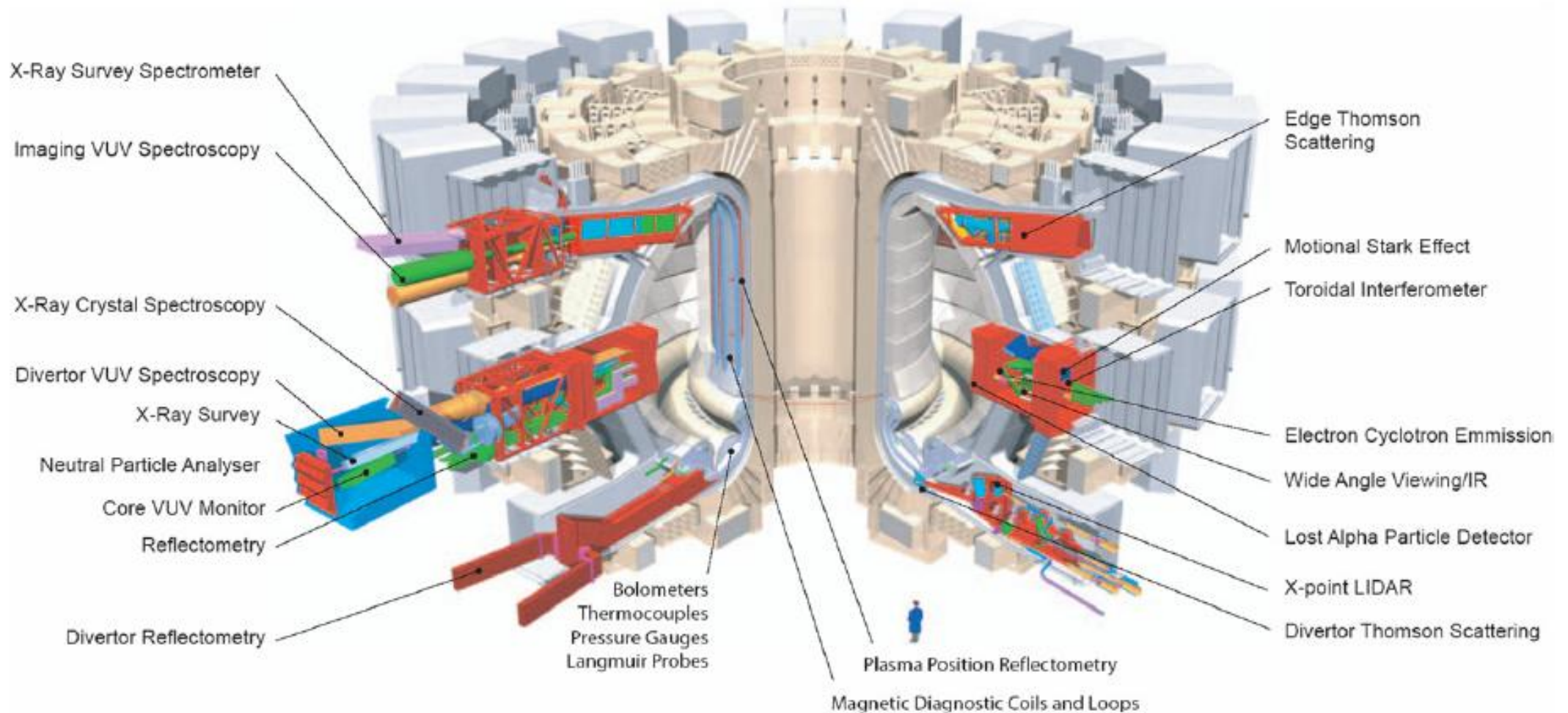
B-field: several teslas

Edge & divertor :

- temperatures down to 1 eV, and less
- a large amount of neutrals can be present (“detached regime”)
- strong atomic line radiation

# An extensive set of diagnostics for ITER

See Progress in the ITER Physics Basis, Nucl. Fusion special issue (2007)



Spectroscopic observations are done in a wide wavelength range: IR, visible, X...  
Passive and active methods are used



# An extensive set of diagnostics for ITER

## Spectral Regions Relevant to Spectroscopy of Magnetically Confined Plasmas

Spectral Region	Wavelength/Energy Region
Near infrared	700 to 1200 nm/1 to 2 eV
Visible	400 to 700 nm/2 to 3 eV
Ultraviolet	200 to 400 nm/3 to 6 eV
Vacuum ultraviolet	30 to 200 nm/6 to 40 eV
Extreme ultraviolet	10 to 30 nm/40 to 120 eV
Soft X-ray	0.1 to 10 nm/120 to 12000 eV

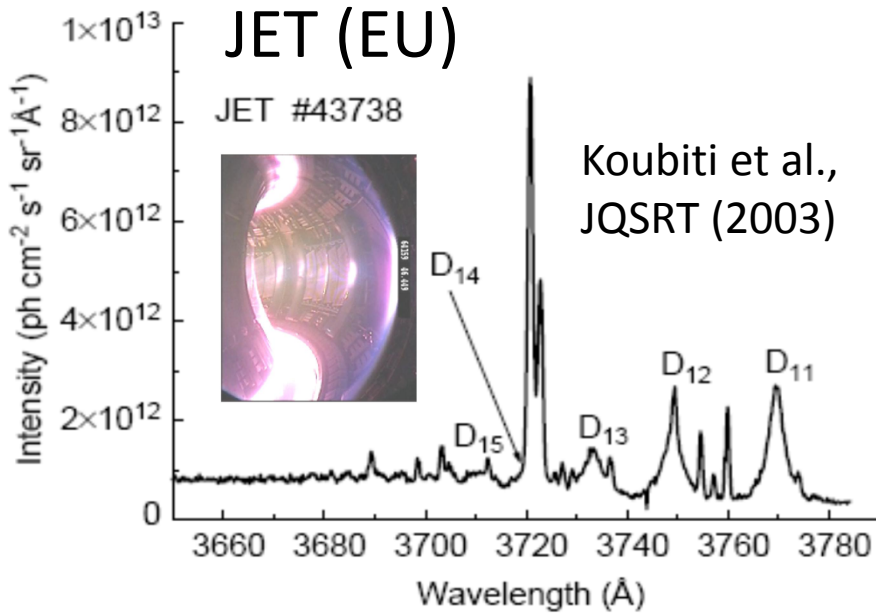
# Passive spectroscopy in current tokamaks

An analysis of line shapes, line widths, line intensities provides information on the plasma parameters

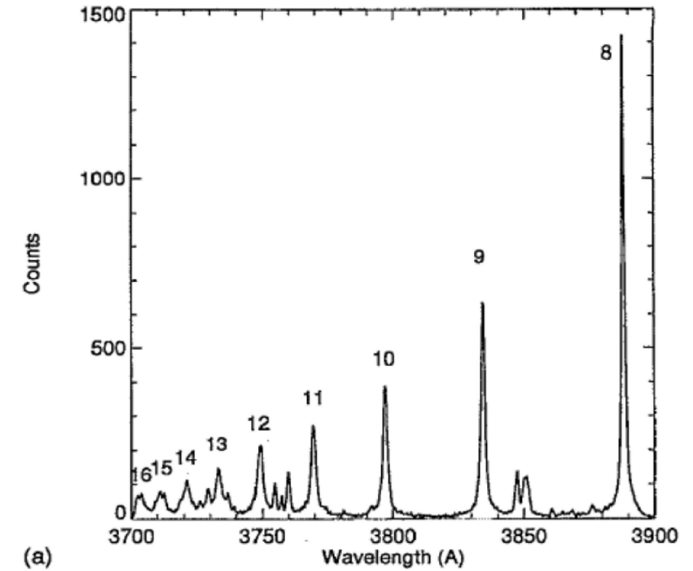
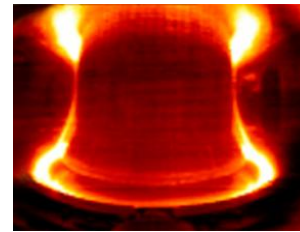
All elements are considered:

- neutral atoms and molecules (edge region, divertor)
- multicharged impurity ions (core region)

# Hydrogen line spectra in tokamak edge and divertor plasmas

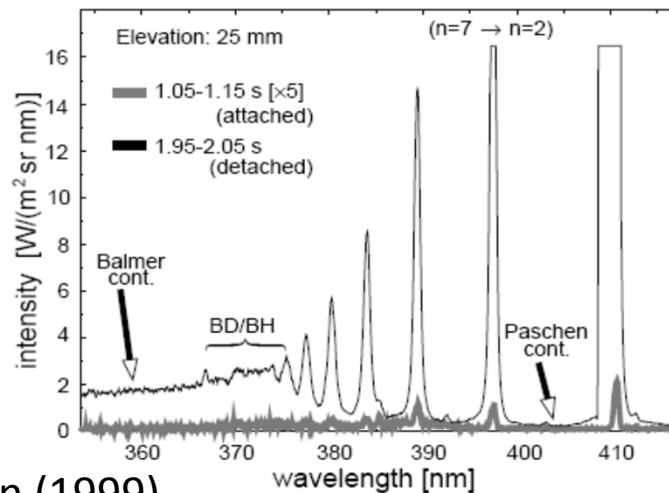


Alcator  
C-Mod (US)

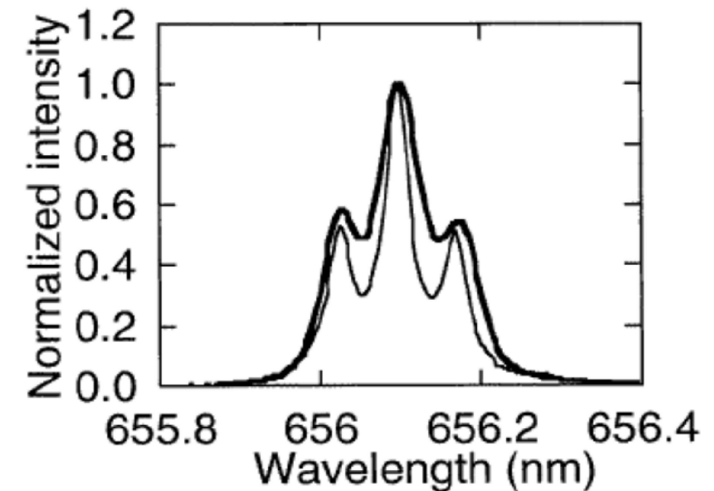


Welch et al., PoP (1995)

ASDEX  
Upgrade  
(Germany)



JT-60U  
(Japan)



Kubo et al., PPCF (1998)

Wenzel et al., Nucl. Fusion (1999)

# Hydrogen line spectra in tokamak edge and divertor plasmas

Lines with a high principal quantum number have been observed in recombining (“detached”) divertor plasma conditions

Their width provides information on the electron density from Stark broadening analysis

The profile of lines with a low principal quantum number (especially Balmer  $\alpha$ ) is usually dominated by Doppler broadening and Zeeman splitting

An analysis of the shape provides information on the neutral velocity distribution function  $f(v)$  in the edge region

# Problematic issues for ITER

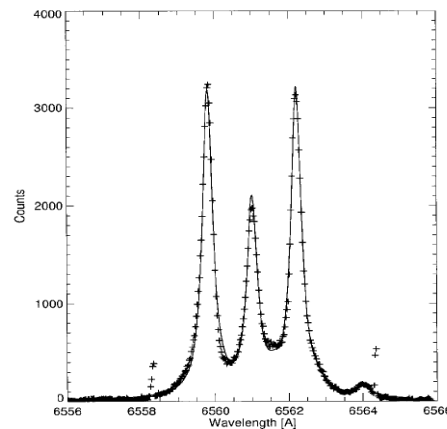
The divertor will be of large size

Can one obtain local information on the plasma parameters?

The density will be sufficiently high so that low-n lines will be affected by both Doppler and Stark effects

Can one extract reliable information on the neutrals' VDF  $f(v)$  from Doppler analysis?

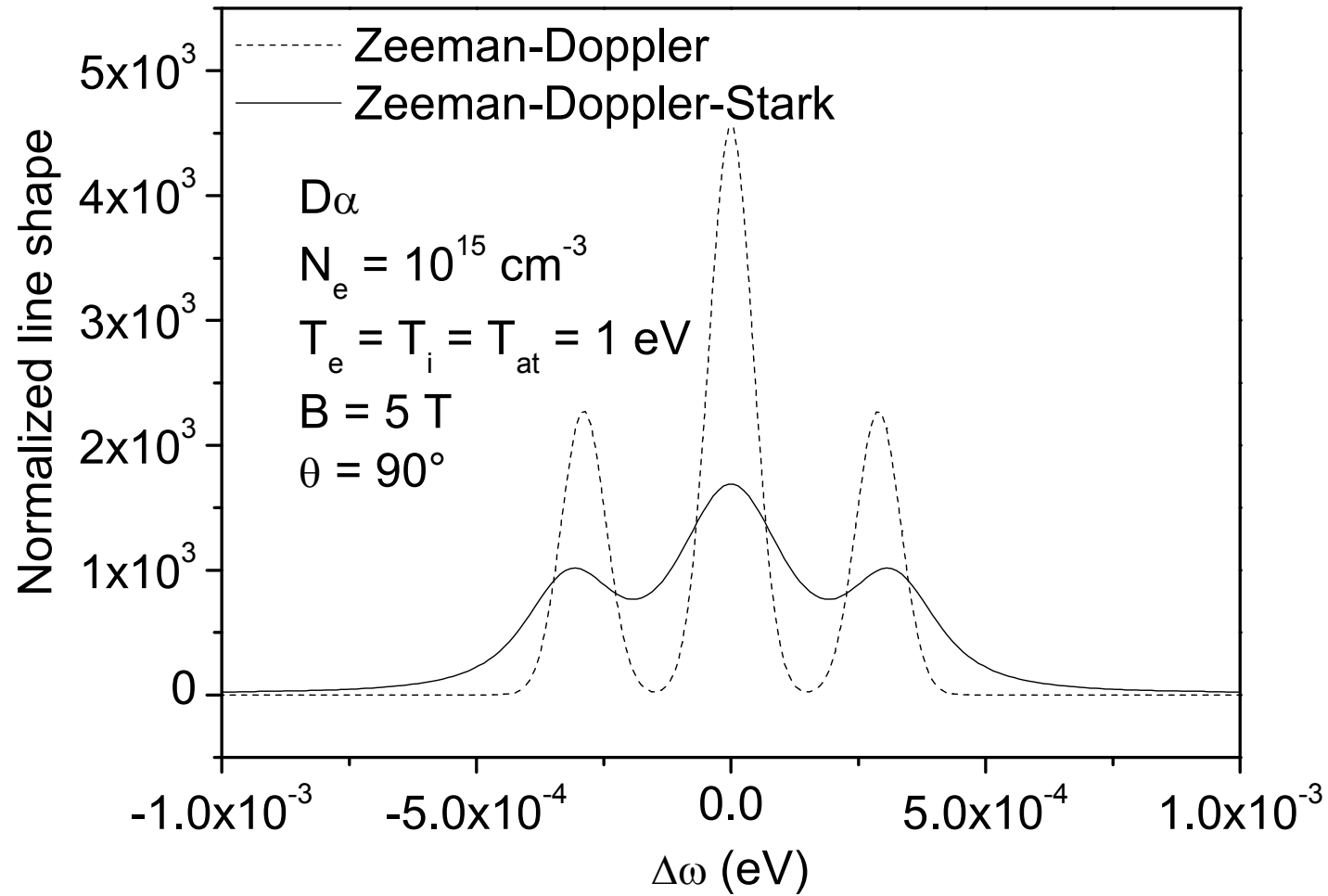
Already problematic  
in Alcator C-Mod



D $\alpha$  Zeeman-Lorentz triplet:  
both Doppler & Stark effects  
contribute to the broadening

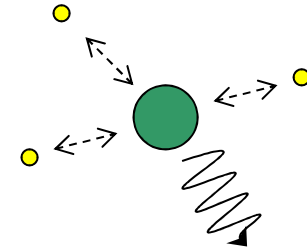
Welch et al., PoP (2001)

# Problematic issues for ITER



# Stark broadening modeling

Stark broadening: when emitting a photon, an atom feels the presence of the charged particles located at vicinity



According to classical textbooks and articles (Baranger, Griem), the Stark-broadening problem amounts to solve the time-dependent Schrödinger equation for the evolution operator  $U(t)$

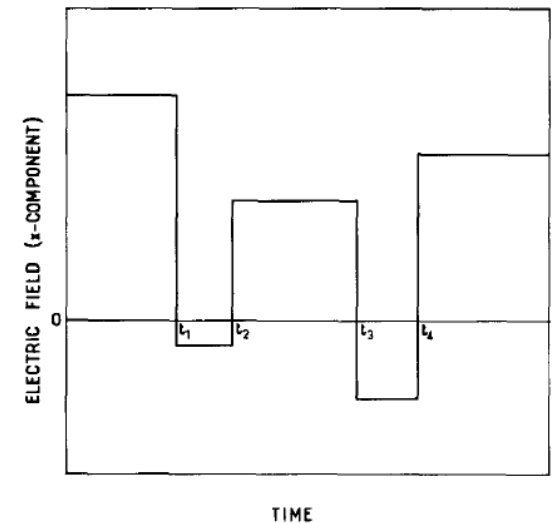
$$i\hbar \frac{dU}{dt}(t) = (H_0 - \vec{d} \cdot \vec{E}(t))U(t)$$

A formal solution can be written using the Dyson series, but there is no explicit form applicable in a general case

# Models and methods for ion dynamics

MMM (Model Microfield Method, 1970s):

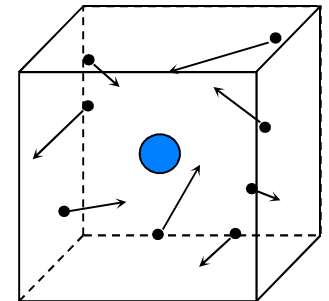
- the E-field is described using a stochastic process
- the Schrödinger equation has an exact solution but this is not the true field



FFM (Frequency Fluctuation Model, 1990s)

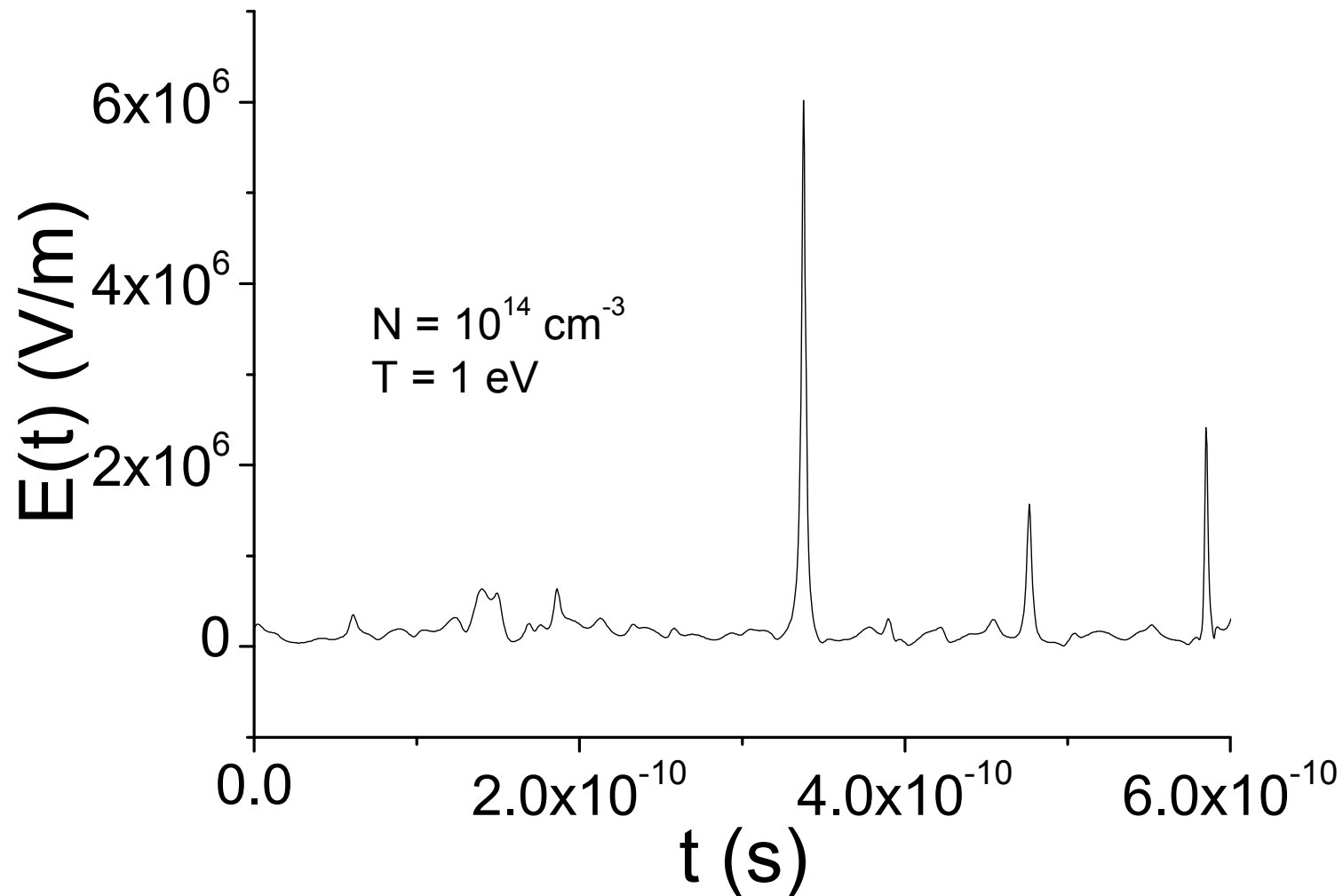
Numerical simulation (1970s):

- particle motion is simulated and the Schrödinger Eq. is solved numerically
- this method is more accurate (benchmark)
- it is time consuming



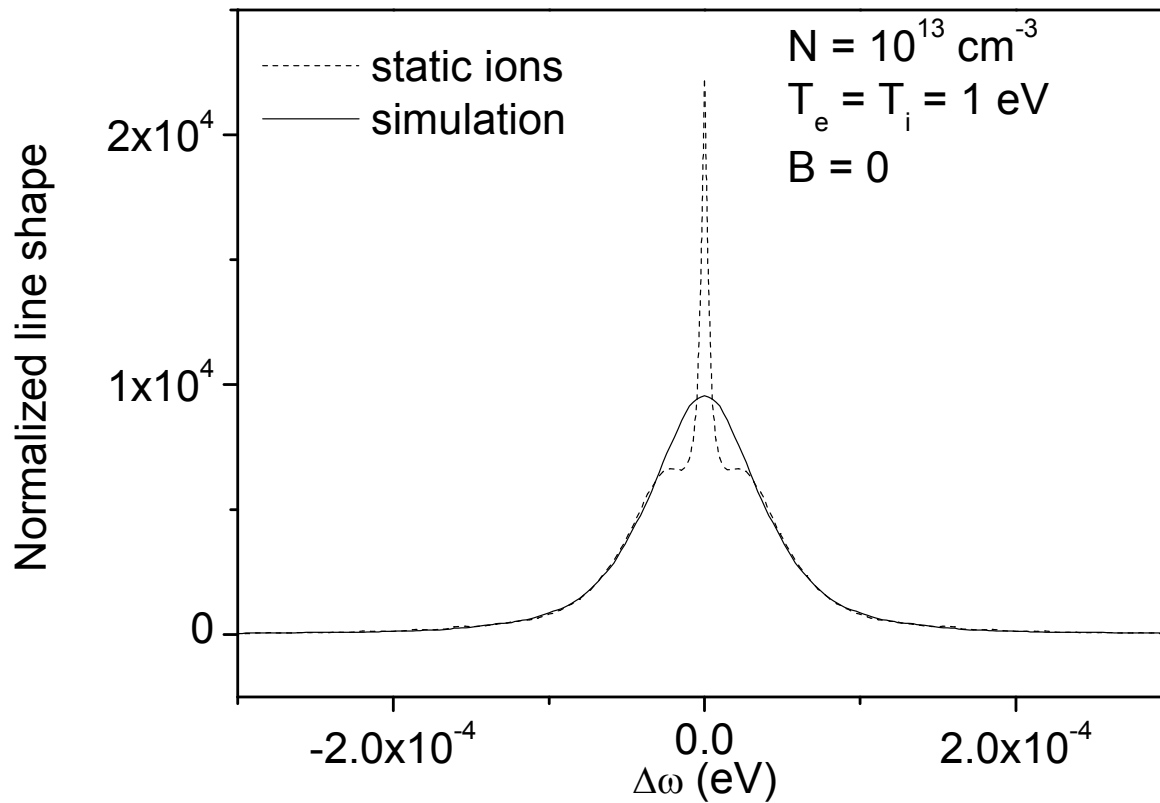


# Models and methods for ion dynamics



# Models and methods for ion dynamics

D $\gamma$  line (deuterium Balmer  $\gamma$ )



The ion dynamics yields  
additional broadening

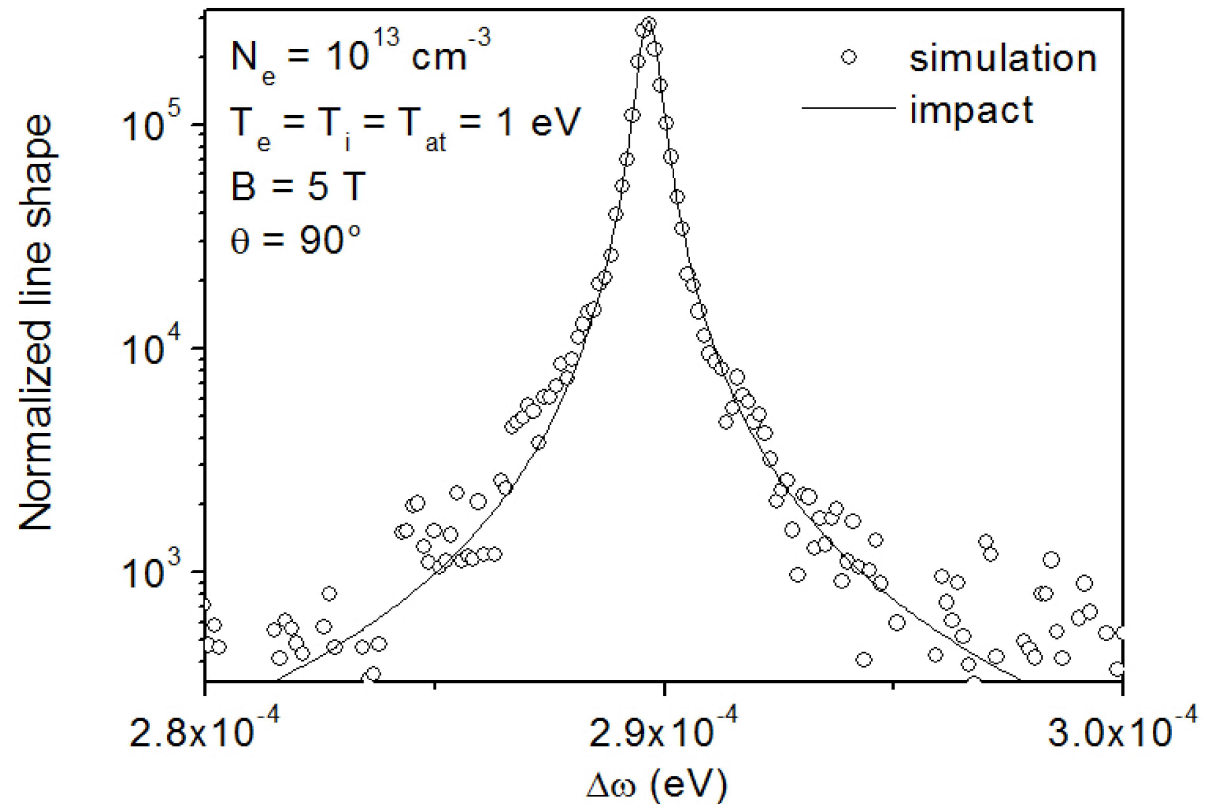
# Models and methods for ion dynamics

Under high dynamics conditions (low  $n$  / low  $N_e$  / high  $T$ ), numerical simulations are time consuming

The use of an impact collision operator for ions can be relevant  
See talk by R. Stamm tomorrow for a discussion

In general, all methods are complementary to each other; they can be tested by performing calculations under suitably chosen plasma conditions (e.g. SLSP code workshop, E. Stambulchik)

Ly  $\alpha$  lateral (Doppler free) Zeeman component

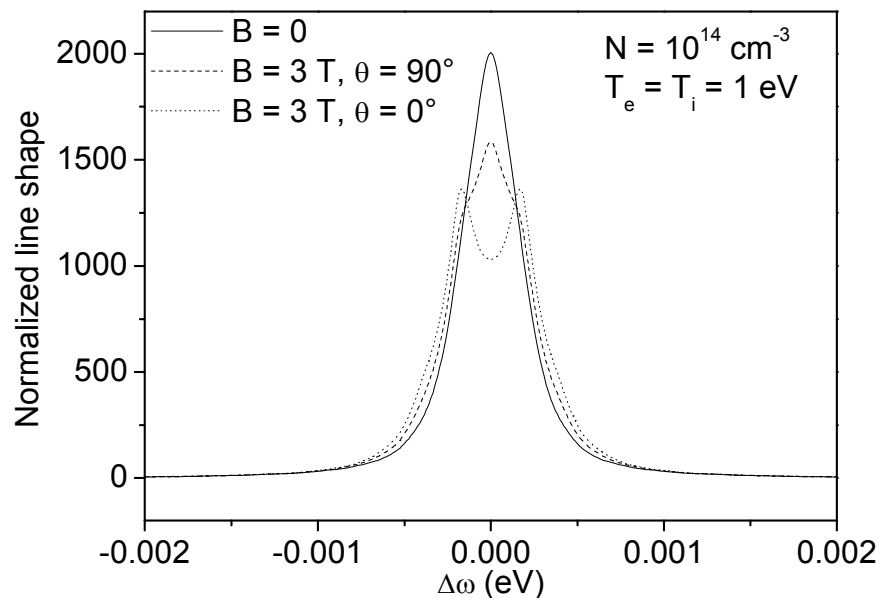


# A database for ITER and current tokamaks



Tables for the first Balmer lines have been constructed using the numerical simulation method:  
from  $D\alpha$  to  $D\epsilon$

- \*  $T_e = T_i = 0.316, 1, 3.16, 10, \text{ and } 31.6 \text{ eV};$
- \*  $N = (1, 2.15, 4.64) \times (10^{13}, 10^{14}, 10^{15}), \text{ and } 10^{16} \text{ cm}^{-3};$
- \*  $B = 0, 1, 2, 2.5, 3, \text{ and } 5 \text{ T}.$



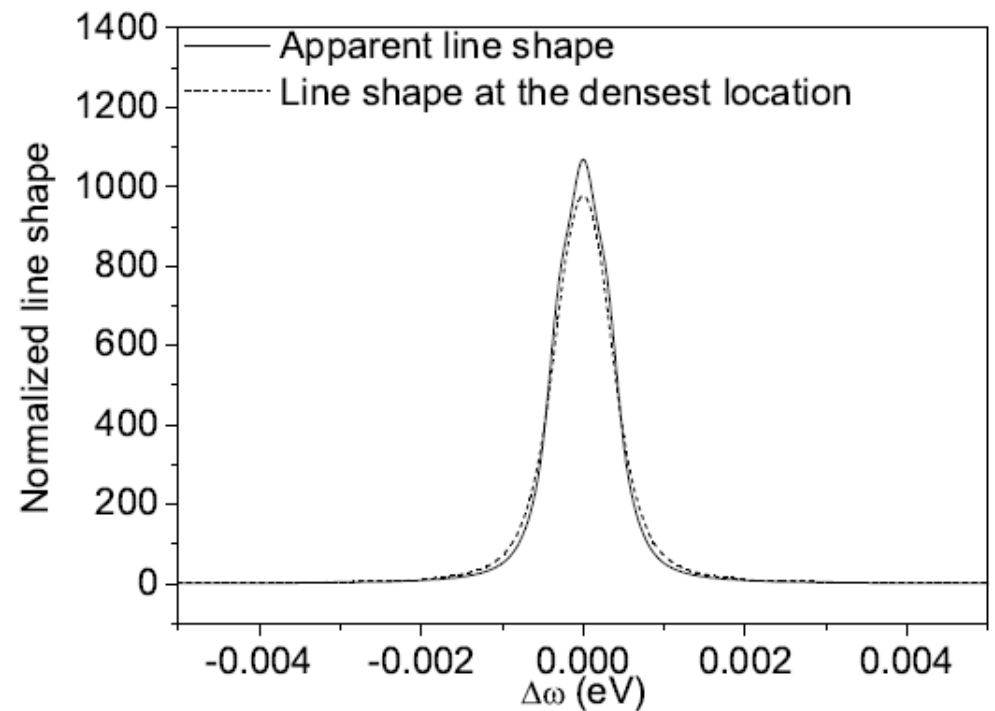
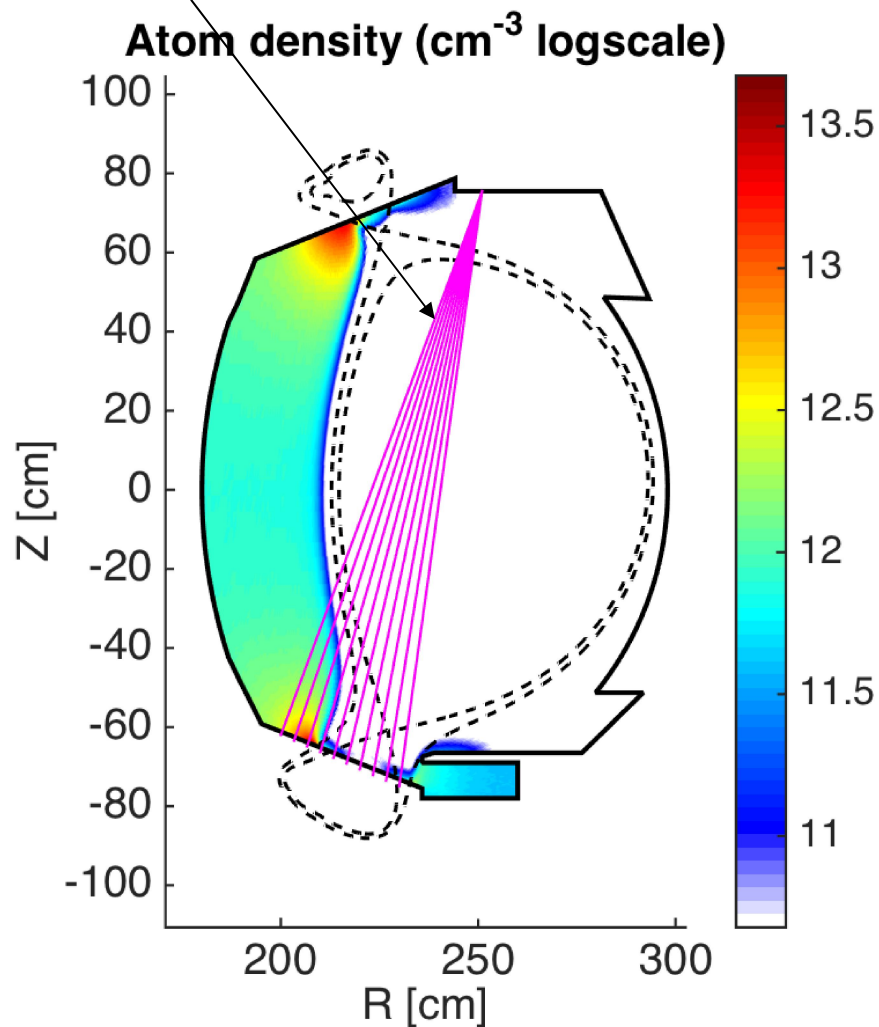
J. Rosato et al., JQSRT 187, 333 (2017)

A FORTRAN program  
that reads the database is ready for use

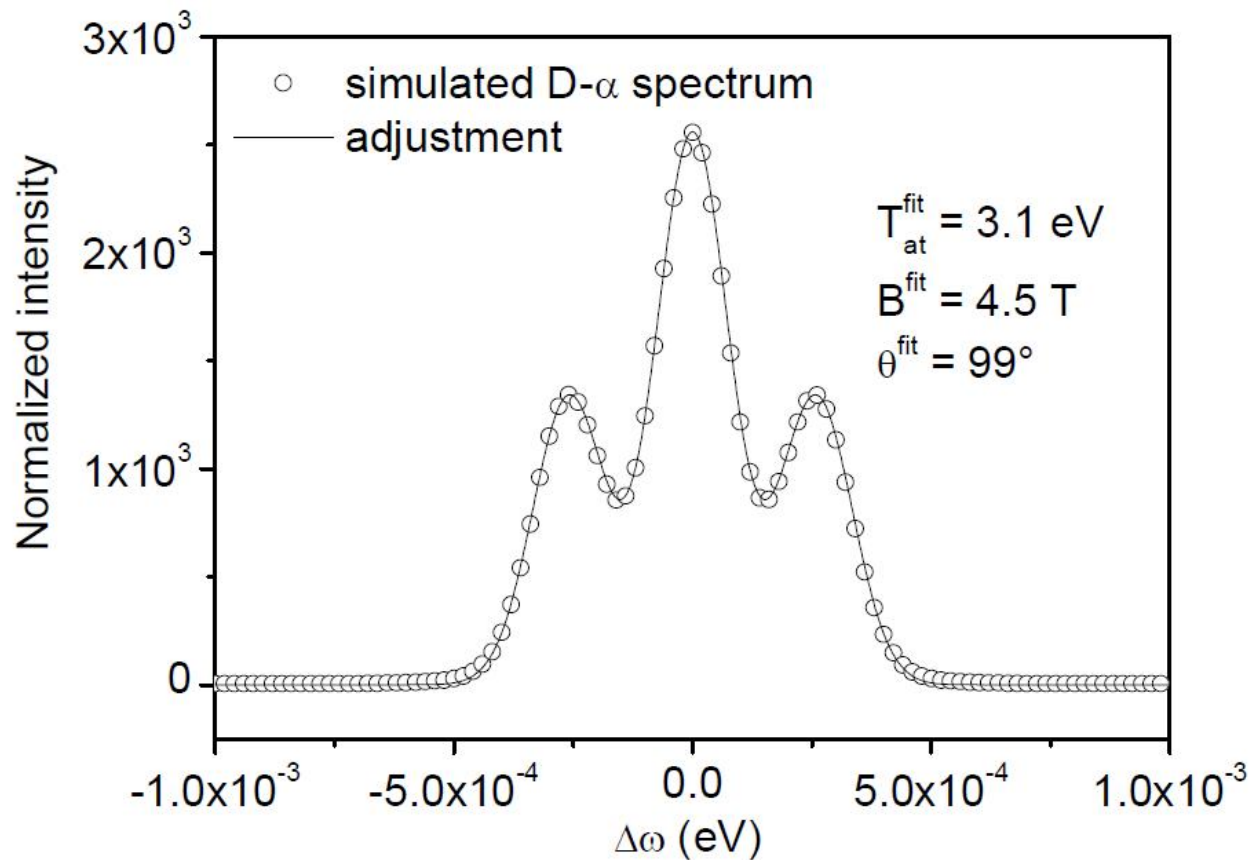
# Simulations of observable spectra

WEST tokamak (France)

Lines of sight



# An analysis of $D\alpha$ observed in a simulated tokamak edge plasma

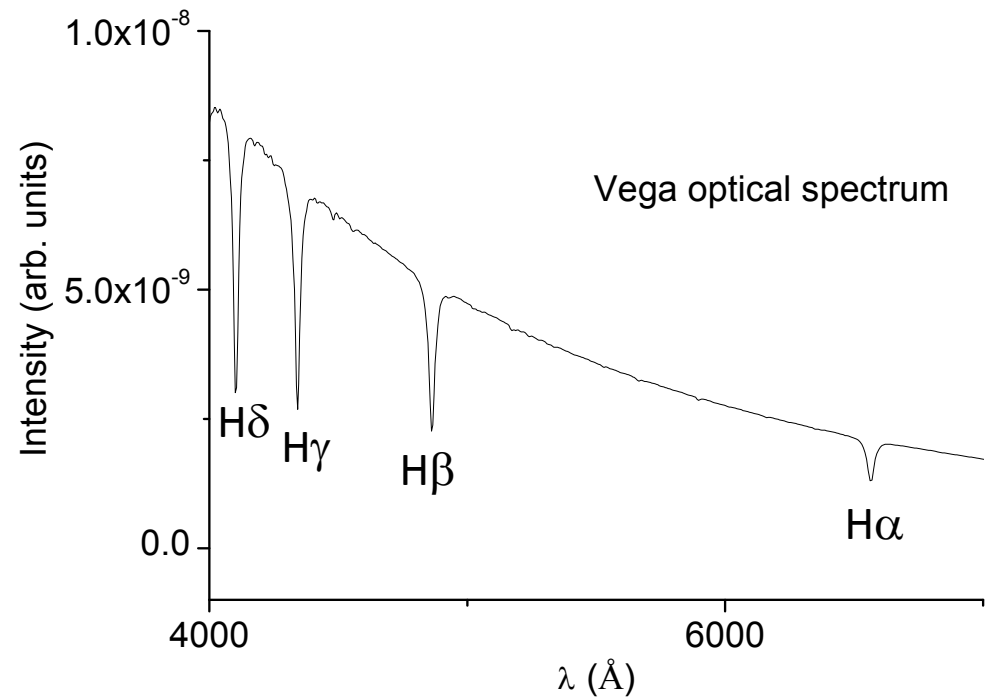


Information on the densest location has been obtained  
Here, the adjustment assumes a Zeeman-Doppler model

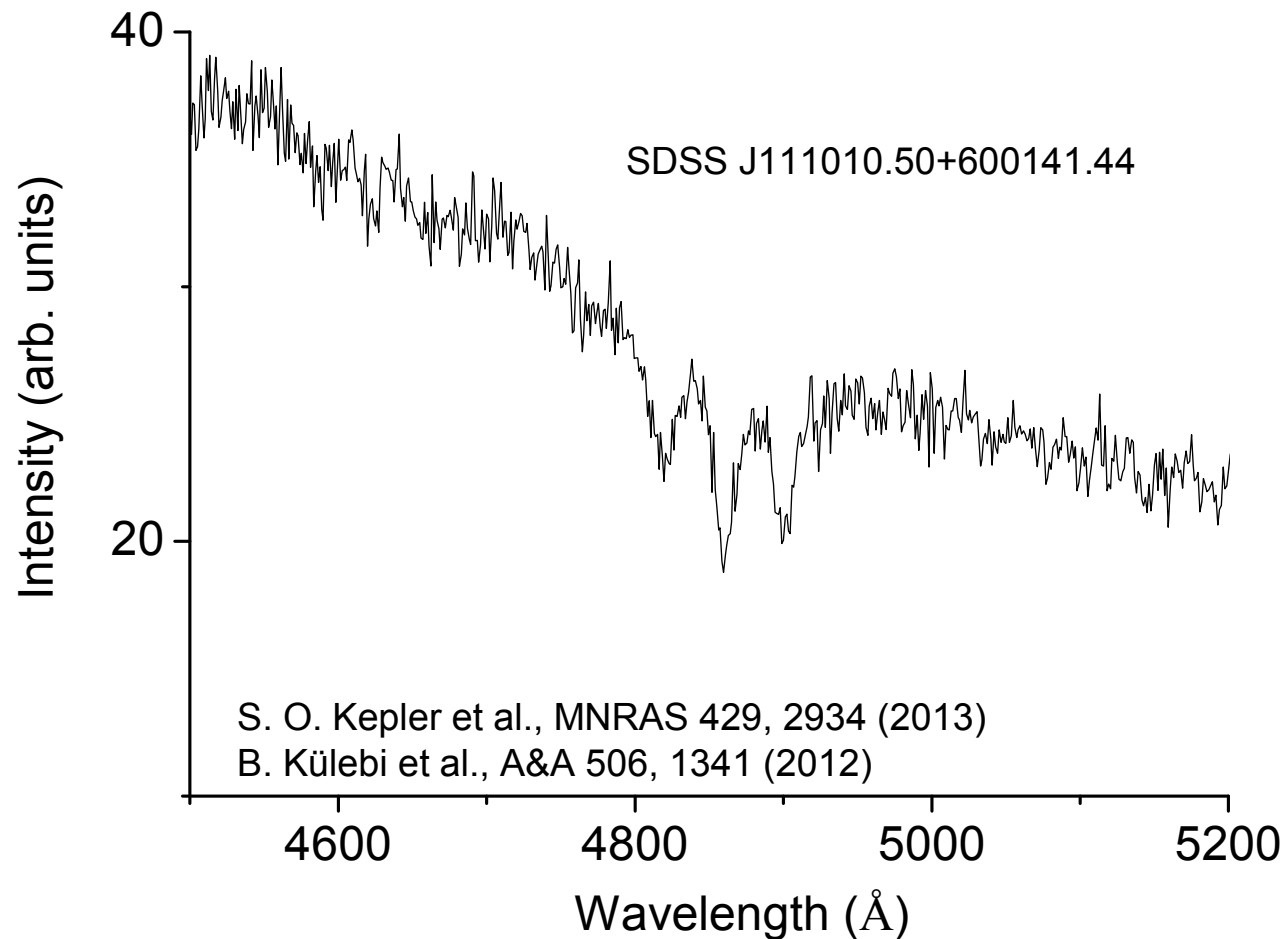
# Adapting the line shape models to stellar atmospheres

In stellar atmospheres, the temperature is low enough so that there is a significant amount of neutrals

The spectrum of A type stars presents hydrogen absorption lines which can be analyzed using the same tools as in magnetic fusion



# Zeeman splitting in magnetic white dwarfs (N. Kieu et al., poster 13)

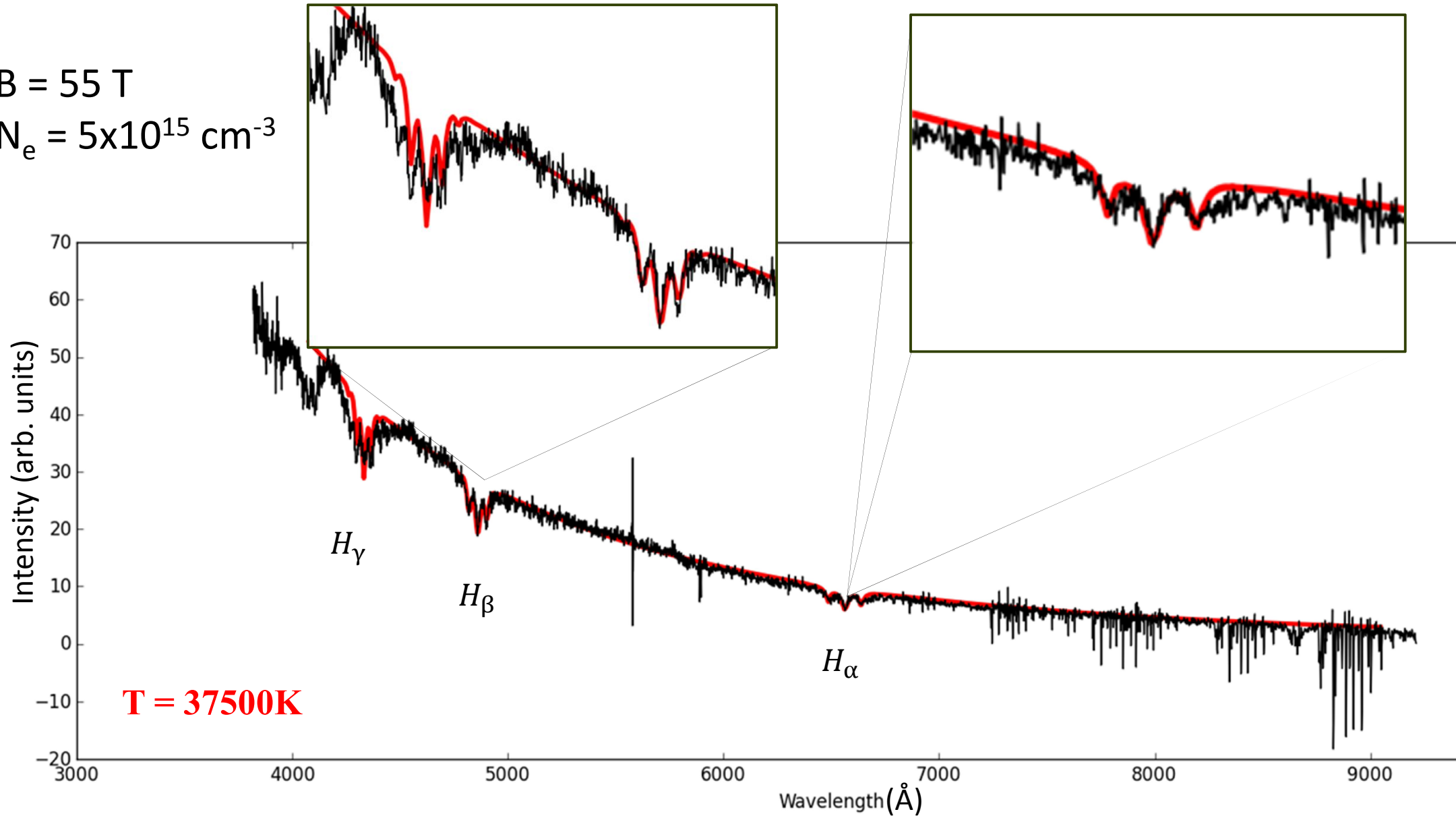




# Line shape fitting

$B = 55 \text{ T}$   
 $N_e = 5 \times 10^{15} \text{ cm}^{-3}$

$B = 100 \text{ T}$   
 $N_e = 5 \times 10^{16} \text{ cm}^{-3}$



# Summary

1) Atomic spectroscopy can be used as a diagnostic for tokamak edge and divertor plasmas  
Models involve both atomic and plasma physics

2) A problem inherent to hydrogen line shape modeling concerns the description of Stark broadening

3) Models can be applied both to magnetic fusion and astrophysics